

EE540 Advance Electromagnetic Theory & Antennas

Prof. Rakesh Singh Kshetrimayum
Dept. of EEE, IIT Guwahati, India

Slot antennas

- *Applications:*
- Low-profile or flush mountings such as in high-speed aircrafts
- *Analysis:*
- Consider complimentary forms such as strips or wires
- Impedances can be found by applying extension of Babinet's (Ba-bi-nay's) principle by Henry Booker
- Patterns can be found by applying duality theorem
- *Babinet's principle in optics:*
- The field at any point behind a plane having a screen,
- if added to the field at the same point
 - when the complementary screen is substituted
- is equal to the field when no screen is present

Slot antennas

Fig. Illustration of Babinet's
(Ba-bi-nay's) Principle

- Assume screen is perfectly absorbing
- Arrangement of a source

& two imaginary planes: P_s and P_o

- Three cases:

- Case I:

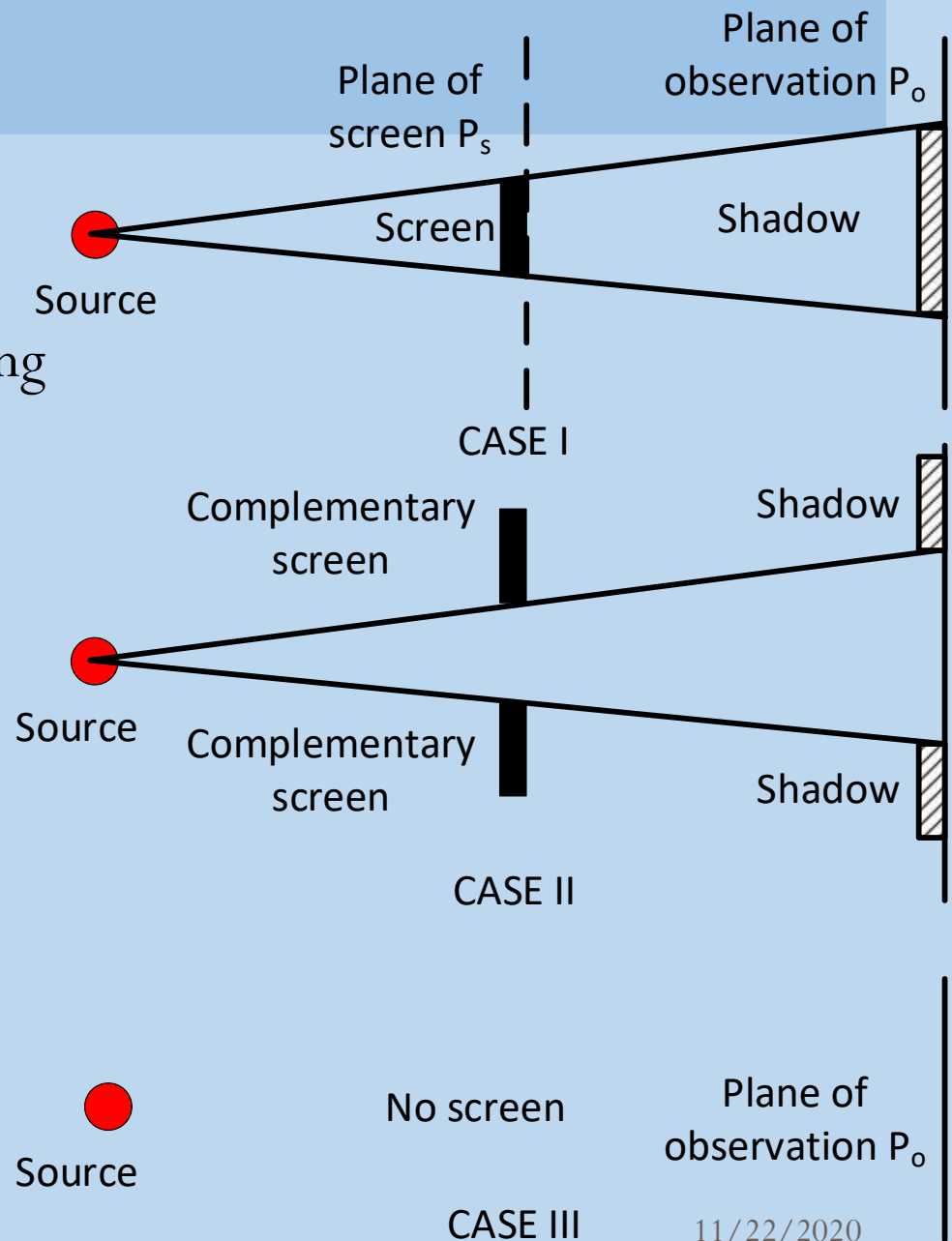
Field at P_o : $F_s = f_1(x, y, z)$

- Case II:

Field at P_o : $F_{cs} = f_2(x, y, z)$

- Case III:

Field at P_o : $F_{ns} = f_3(x, y, z)$



Slot antennas

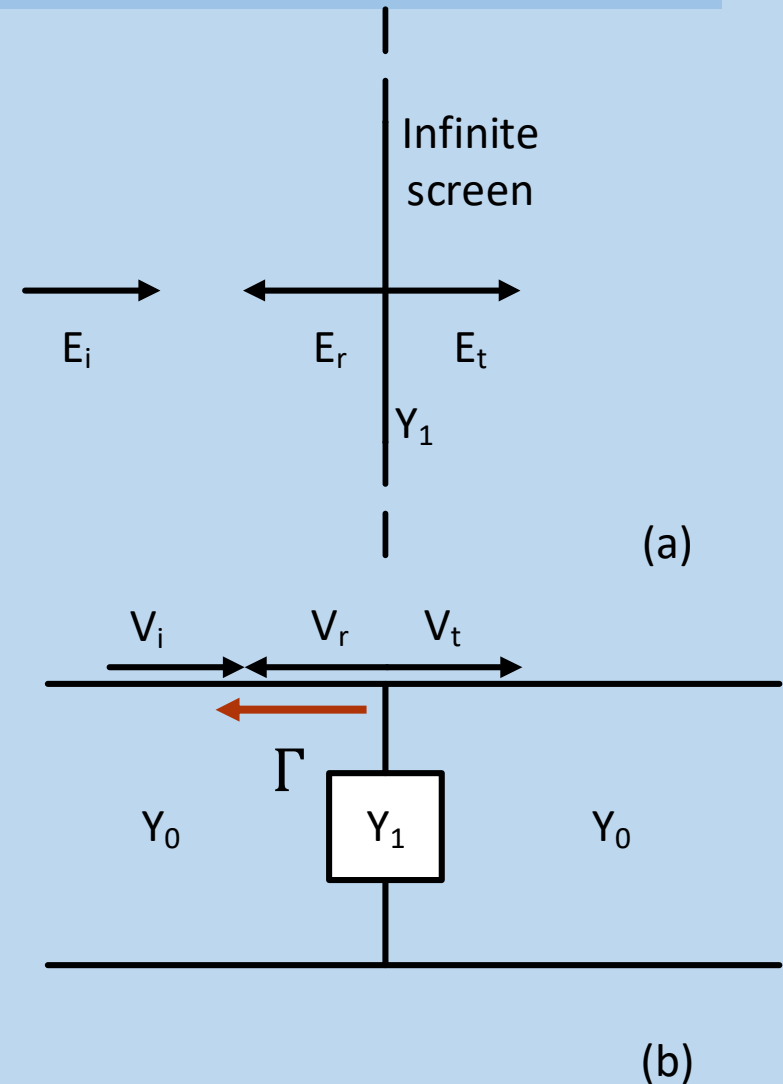
- Babinet's principle asserts that the field for the third case without screen
- is equal to the sum of the fields in the first and second cases
 - $f_3(x,y,z) = f_1(x,y,z) + f_2(x,y,z)$
- The P_o can be anywhere behind the P_s
- Henry Booker extended this principle in 1946 to antennas
- In antenna analysis,
 - if the screen is PEC
 - then the complementary screen is PMC
- The analysis of Babinet's principle
 - can be done with the help of transmission line analogy

Slot antennas

- Fig. (a) A plane wave of field intensity E_i is incident on an infinite screen of surface admittance Y_1
- (b) A wave of voltage V_i incident on an infinite transmission line loaded with a shunt admittance Y_1 placed across the line placed across the line

$$\Gamma = \frac{Z_L - Z_0}{Z_L + Z_0} = \frac{\frac{1}{Y_L} - \frac{1}{Y_0}}{\frac{1}{Y_L} + \frac{1}{Y_0}} = \frac{Y_0 - Y_L}{Y_L + Y_0}$$

$$\because Y_L = Y_1 + Y_0 \quad \therefore \Gamma = \frac{Y_0 - Y_1 - Y_0}{Y_1 + Y_0 + Y_0} = \frac{-Y_1}{Y_1 + 2Y_0}$$



Slot antennas

- We can find the transmission coefficient
- $\tau = 1 + \Gamma = 1 + \frac{-Y_1}{Y_1 + 2Y_0} = \frac{Y_1 + 2Y_0 - Y_1}{Y_1 + 2Y_0} = \frac{2Y_0}{Y_1 + 2Y_0}$
- Consider two cases:
- Case I: PEC infinite screen surface admittance Y_1
- Then $\tau_1 = \frac{2Y_0}{Y_1 + 2Y_0}$
- Case II: PMC infinite screen surface admittance Y_2
- Then $\tau_2 = \frac{2Y_0}{Y_2 + 2Y_0}$
- According to Babinet's principle,
- sum of the above two cases would be equal to that the case
- when there are no infinite screen, hence $\tau_1 + \tau_2 = 1$

Slot antennas

- $\tau_1 + \tau_2 = 1$ means that
- $\frac{2Y_0}{Y_1+2Y_0} + \frac{2Y_0}{Y_2+2Y_0} = 1$
- $\Rightarrow 2Y_0(Y_2+2Y_0) + 2Y_0(Y_1+2Y_0) = (Y_2+2Y_0)(Y_1+2Y_0)$
- $\Rightarrow 2Y_0Y_2+8Y_0^2 + 2Y_0 Y_1 = Y_2Y_1 + 2Y_0Y_2 + 2Y_0Y_1 + 4Y_0^2$
- $\Rightarrow 4Y_0^2 = Y_2Y_1$
- which is the *Booker's relation for admittance*
- In terms of impedance,
- $Z_1Z_2 = \frac{Z_0^2}{4} \Rightarrow \sqrt{Z_1Z_2} = \frac{Z_0}{2}$
- The GM of the surface impedances of the screen in two cases considered is equal to $\frac{1}{2}$ the intrinsic impedance of the surrounding medium (e.g. $Z_0 \cong 377\Omega$ for free space)

Slot antennas

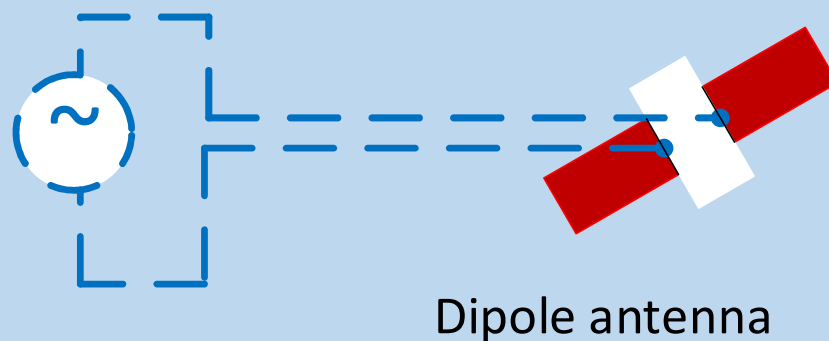
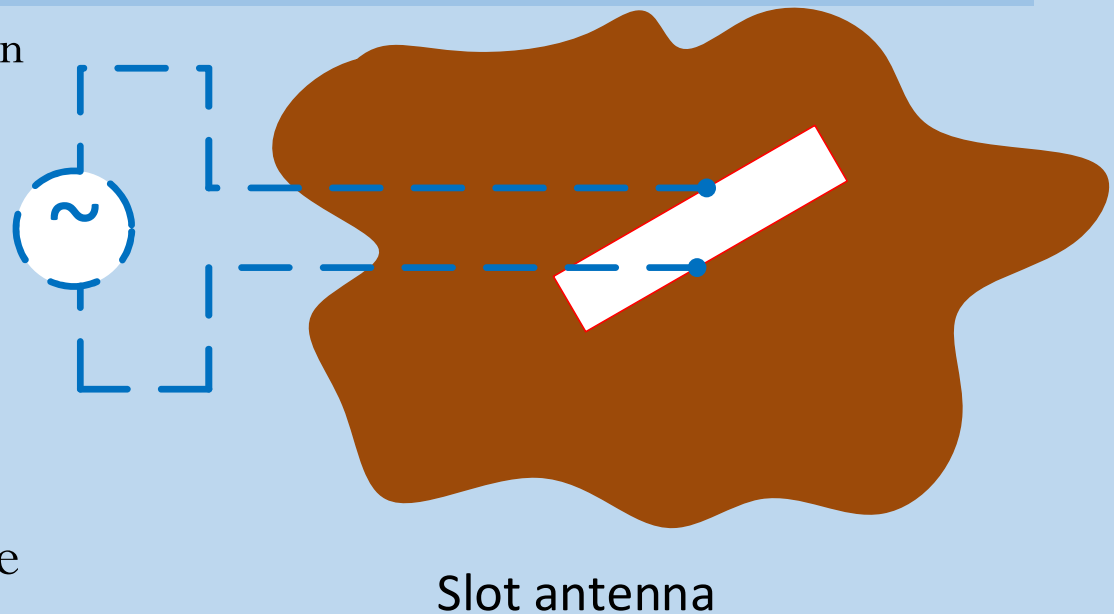
- Fig. Application of Booker's relation for impedance of slot and dipole antenna

- $Z_s Z_d = \frac{Z_0^2}{4}$

- Given the dipole antenna impedance Z_d , one can find the impedance of the corresponding slot antenna as

- $Z_s = \frac{35,476}{Z_d}$

- Note that in general Z_d is complex number

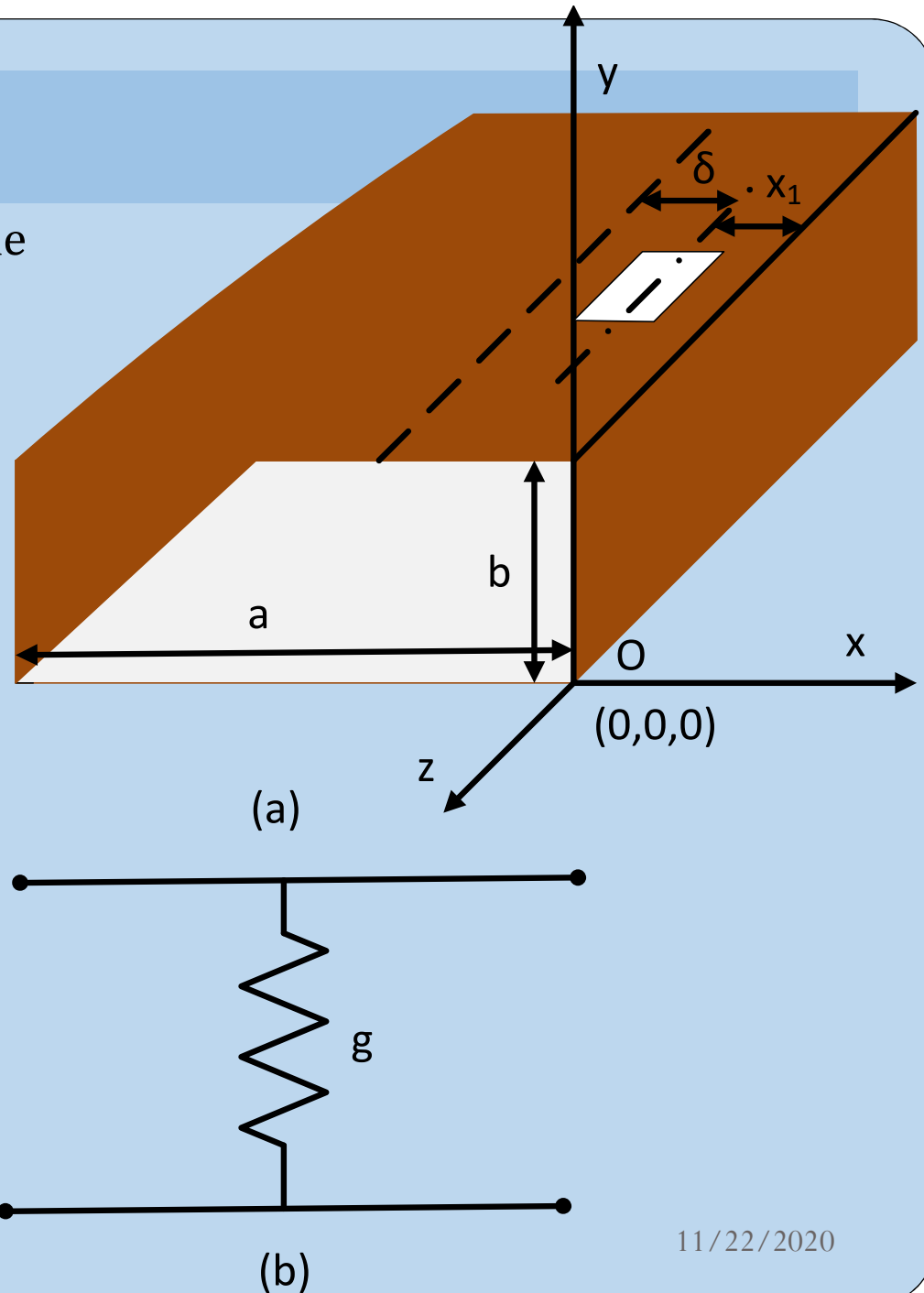


Slot antennas

- Half-wavelength dipole ($2L = \frac{\lambda}{2}$) FF radiation pattern (from lecture 18)
- $$E_{\theta} \cong j\eta \frac{I_0 e^{-j\beta r}}{2\pi r} \left[\frac{\cos(\beta L \cos\theta) - \cos(\beta L)}{\sin\theta} \right] = j\eta \frac{I_0 e^{-j\beta r}}{2\pi r} \left[\frac{\cos\left(\frac{\pi}{2} \cos\theta\right)}{\sin\theta} \right]$$
- $$H_{\phi} \cong j \frac{I_0 e^{-j\beta r}}{2\pi r} \left[\frac{\cos\left(\frac{\pi}{2} \cos\theta\right)}{\sin\theta} \right]$$
- Application of Duality principle
- Half-wavelength slot ($2L = \frac{\lambda}{2}$) FF radiation pattern
- $$H_{\theta} \cong j \frac{I_m e^{-j\beta r}}{\eta 2\pi r} \left[\frac{\cos\left(\frac{\pi}{2} \cos\theta\right)}{\sin\theta} \right]$$
- $$E_{\phi} \cong -j \frac{I_m e^{-j\beta r}}{2\pi r} \left[\frac{\cos\left(\frac{\pi}{2} \cos\theta\right)}{\sin\theta} \right]$$
- Another very popular slot antenna is **slotted waveguide antenna and arrays** also called as travelling wave slot antenna and arrays

Slot antennas

- Fig. (a) Shunt slot in waveguide
- (b) Equivalent circuit
- $g = \frac{Y_s}{Y_0}$
- where g is normalized shunt conductance,
- Y_s is the shunt admittance of the slot in the waveguide and
- Y_0 is the characteristic admittance of the waveguide

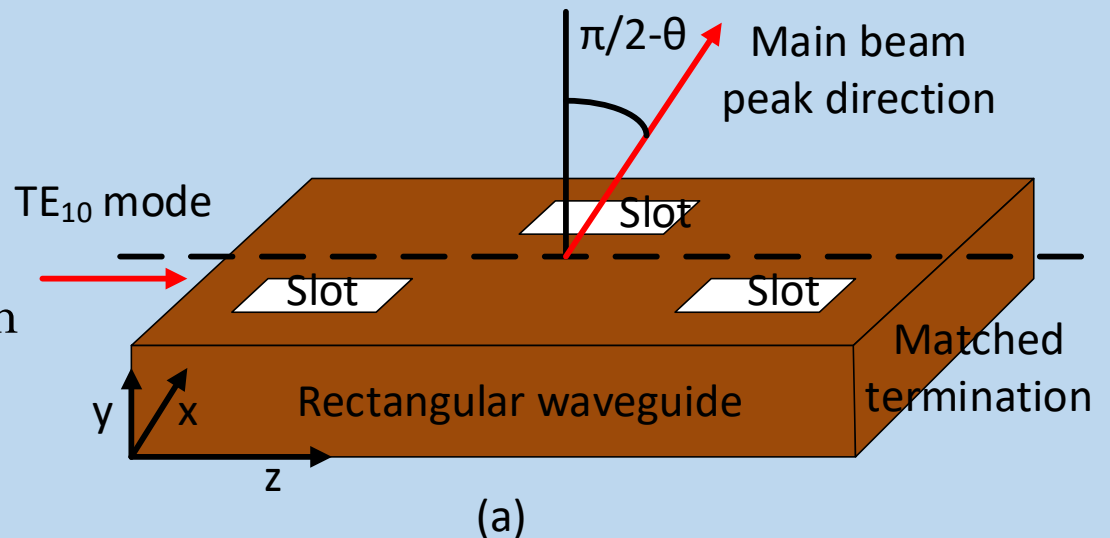


Slot antennas

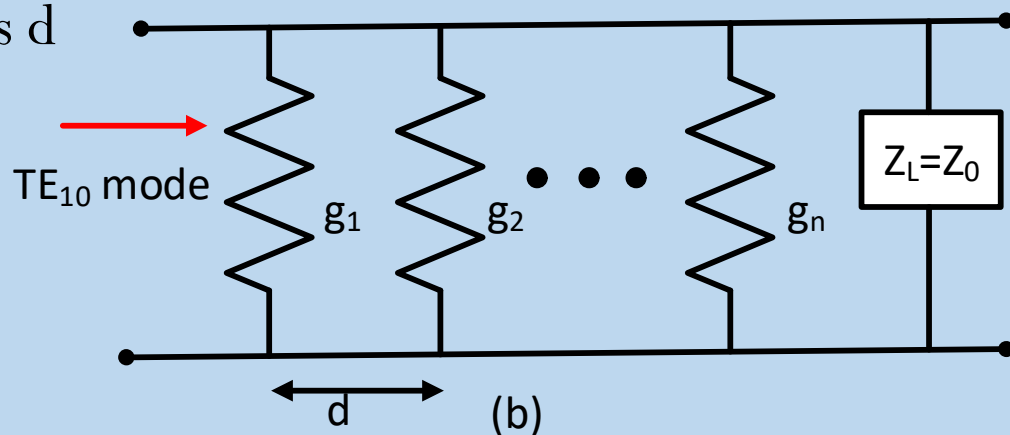
- $g = 2.09 \frac{\lambda_g a}{\lambda_0 b} \cos^2 \left(\frac{\pi \lambda_0}{2 \lambda_g} \right) \sin^2 \left(\frac{\pi \delta}{a} \right)$
- where
- λ_g is the guided wavelength of the dominant TE_{10} mode inside the waveguide $\left(\lambda_{g10} = \frac{2\pi}{\beta_{10}} = \frac{2\pi}{\sqrt{\beta^2 - \left(\frac{\pi}{a}\right)^2}} > \lambda_0 \right)$
- λ_0 is the free space wavelength
- a and b are the dimension of the waveguide
- $\delta = \frac{a}{2} - x_1$ is the slot offset from the central line
 - which determines the slot conductance
 - with zero at the central line and
 - increase square sinusoidally with δ

Slot antennas

- Fig.
- (a) Slotted waveguide antenna array
- (b) Equivalent transmission line model
- Line model



- Separation between slots is d
- Position vector for any i^{th} slot centre is given by
- $\vec{r}_i = x_i \hat{x} + b \hat{y} + id \hat{z}$
- where $i=1,2,\dots,n$
- and x_i is the off-set distance of the i^{th} slot centre from waveguide side wall



Slot antennas

- Height of the waveguide is common for all slots in the waveguide,
- it has no influence on the radiation pattern of the slotted waveguide antenna array
- It can be neglected and hence $\vec{r}_i = x_i \hat{x} + id \hat{z}$
- AF can be calculated as
- $AF = 1 + a_1 e^{j\psi_1} + a_2 e^{j\psi_2} + \dots + a_{n-1} e^{j\psi_{n-1}}$
- where a_i is the field excitation amplitude at the i^{th} slot
- and $\psi_i = \vec{\beta} \cdot \vec{r}_i - i\beta_{10}d + i\pi$
- $-i\beta_{10}d$ is the slot-to-slot phase delay $\left(\beta_{10} = \sqrt{\beta^2 - \left(\frac{\pi}{a}\right)^2} \right)$
- π is phase shift due to the slot staggering (it will disappear if the shunt slots were placed on the same side from the centre line)

Slot antennas

- $\vec{\beta} \cdot \vec{r}_i = (\beta \sin\theta \cos\phi \hat{x} + \beta \sin\theta \sin\phi \hat{y} + \beta \cos\theta \hat{z}) \cdot (x_i \hat{x} + id \hat{z})$
- $= \beta x_i \sin\theta \cos\phi + \beta id \cos\theta$
- $\psi_i = \beta x_i \sin\theta \cos\phi + \beta id \cos\theta - \beta_{10} d + \pi$
- For radiation pattern in y-z plane, $\phi = \frac{\pi}{2}$
- $\psi_i = \beta id \cos\theta - i\beta_{10} d + i\pi$
- AF can be simplified as
- $AF = 1 + a_1 e^{j\psi} + a_2 e^{j2\psi} + \dots + a_{n-1} e^{j(n-1)\psi}$
- where $\psi = \beta d \cos\theta - \beta_{10} d + \pi$
- Main beam is for $\psi = 0$
- Primary lobes: $\psi = \beta d \cos\theta - \beta_{10} d + \pi = 2m\pi$
- where $m=1,2,\dots,M$

Slot antennas

- Hence, primary lobes occur at values of the slot spacing d given by:

$$\psi = \beta d \cos\theta - \beta_{10}d + \pi = 2m\pi$$

- where $m=1,2,\dots,M$

- $$\frac{2\pi}{\lambda} d \cos\theta - \frac{2\pi}{\lambda_{g10}} d + \pi = 2m\pi$$

- $$\Rightarrow d \left(\frac{1}{\lambda} \cos\theta - \frac{1}{\lambda_{g10}} \right) = \frac{(2m-1)}{2}$$

- $$\Rightarrow d \left(\frac{\lambda_{g10} \cos\theta - \lambda}{\lambda \lambda_{g10}} \right) = \frac{(2m-1)}{2}$$

- $$\Rightarrow d = \frac{(2m-1)}{2} \left(\frac{\lambda \lambda_{g10}}{\lambda_{g10} \cos\theta - \lambda} \right)$$

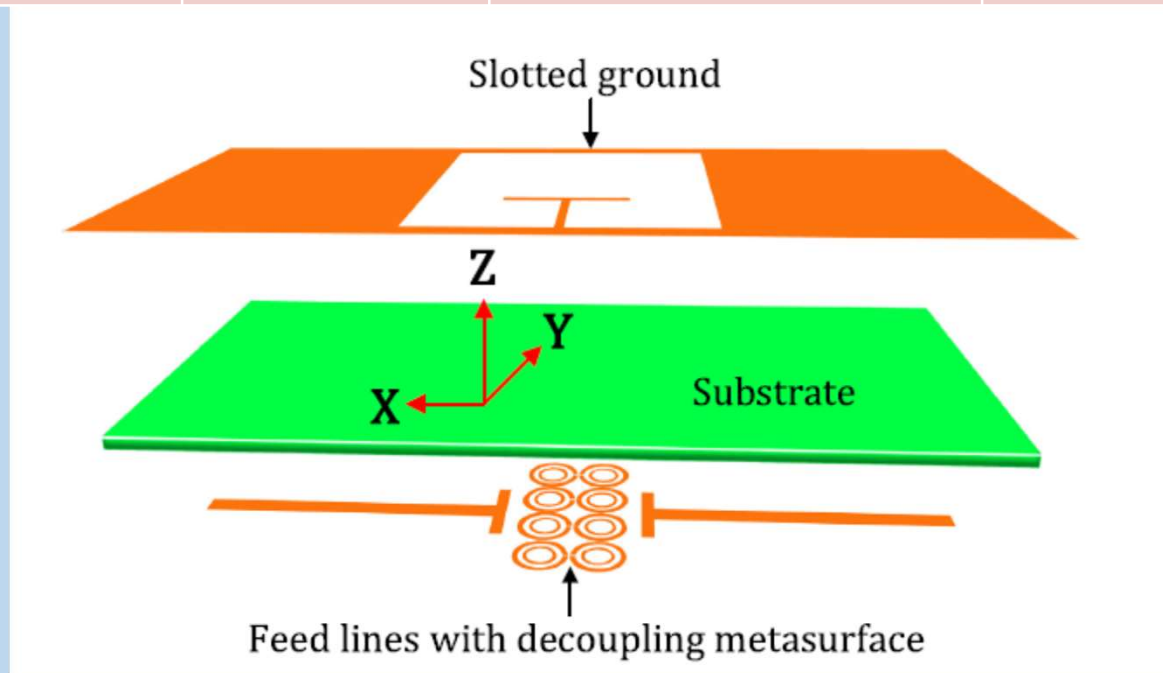
- For $\theta = 0^\circ$,
$$d = \frac{(2m-1)}{2} \left(\frac{\lambda \lambda_{g10}}{\lambda_{g10} - \lambda} \right)$$

Slot antennas

- For $\theta = 180^\circ$, $d = \frac{(1-2m)}{2} \left(\frac{\lambda \lambda_{g10}}{\lambda_{g10} + \lambda} \right)$
- Infinity occurs at $\lambda_{g10} \cos\theta - \lambda = 0$
- $\cos\theta = \frac{\lambda}{\lambda_{g10}}$
- *Some of the slot antenna and arrays from our research group:*
- *All slot antenna and arrays are designed for full-duplex radios*
 - High inter-port isolation Dual circularly polarized (DCP) slot antenna with split ring resonator (SRR) based novel metasurface
 - Series-fed DCP slot antenna array with metallic reflector
 - DCP slot antenna with “8” shaped slots with Interdigital capacitor (IDC)

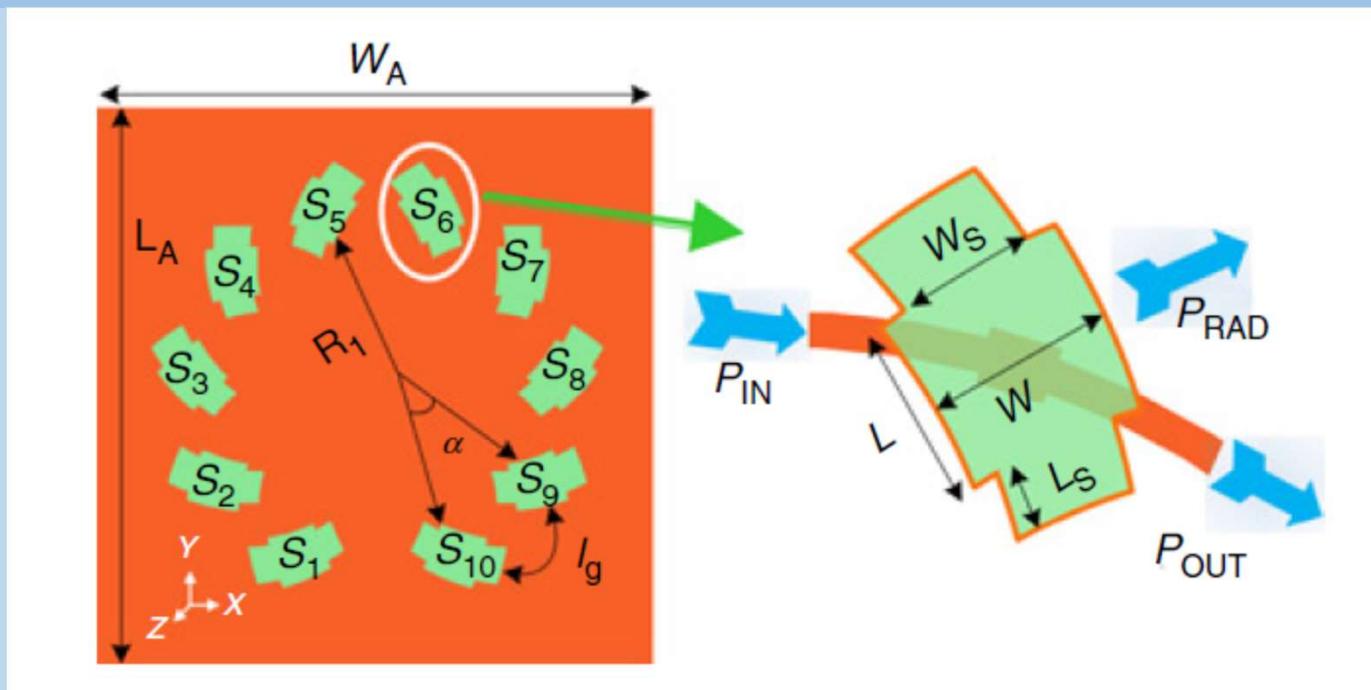
Slot antennas

Isolation (dB)	- 10 dB bandwidth	AR bandwidth	Antenna size	Gain	Radiation pattern
27-36	28.52% ($f_c=6.45\text{GHz}$)	8.9% ($f_c=6.54\text{ GHz}$)	$1.58\lambda_0 \times 0.75\lambda_0 \times 0.024\lambda_0$	2.9 to 3.6 dBic	Bidirectional



- Fig. Slot antenna: High inter-port isolation DCP slot antenna with SRR based novel metasurface (Source: <https://doi.org/10.1016/j.aeue.2019.05.016>)

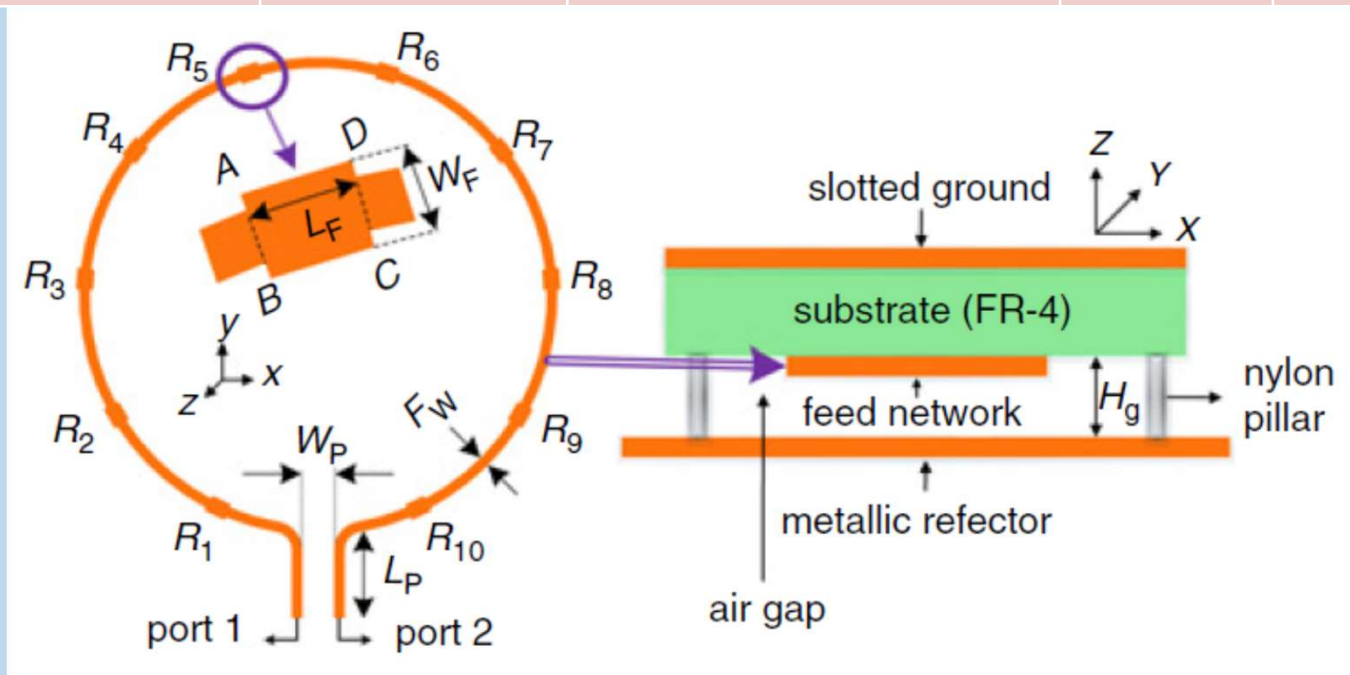
Slot antennas



- Fig. Series-fed DCP slot antenna array: Slotted ground plane with ten slots and radiating single slot model (Source: <https://ieeexplore.ieee.org/document/8855215>)
- First five slots (S_1 to S_5 corresponding to Port 1) contribute to 98.7% of the total power radiated by the antenna for $\gamma=0.57$

Slot antennas

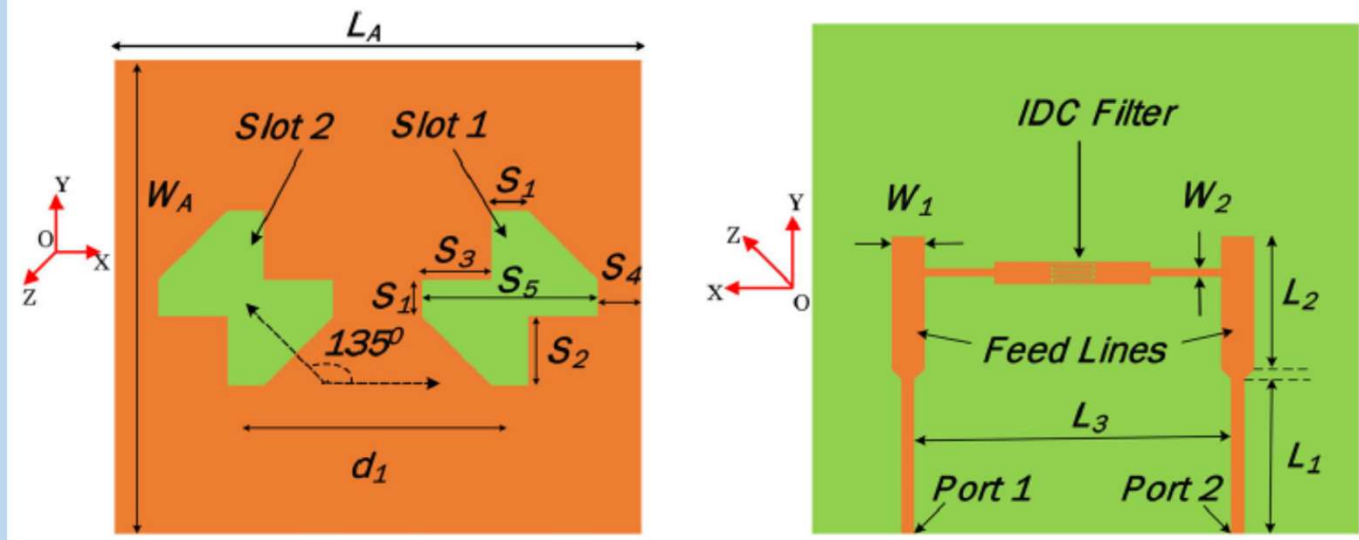
Isolation (dB)	- 10 dB bandwidth	AR bandwidth	Power coupling coefficient	Gain	Radiation pattern
25-45	18.46% ($f_c=6.45\text{GHz}$)	13.46% ($f_c=6.54\text{ GHz}$)	$\gamma=1(S_{21})^2=0.57=P_{\text{out}}/P_{\text{in}}$ of an isolated slot	8.2 to 9.5 dBic	Unidirectional



- Fig. Slot antenna array: Series feed network showing the ports and side-view of the antenna showing the metallic reflector (Source: <https://ieeexplore.ieee.org/document/8855215>)

Slot antennas

Isolation (dB)	- 10 dB bandwidth	AR bandwidth	Antenna size	Gain	Radiation pattern
17.6 to 46	15.75% ($f_c=2.293\text{GHz}$)	11.52% ($f_c=2.1275\text{ GHz}$)	$1.14 \lambda_0 \times 0.91 \lambda_0$	3 to 5 dBic	Bidirectional



- Fig. DCP slot antenna with “8” shaped slots: front and rear view of the antenna (a) slotted ground (b) feed network with IDC
(Source: <https://doi.org/10.1002/mmce.21903>)