On finite and infinite sets

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• A set S is *finite* whenever there exists a bijection from the set [n] to S, for a fixed n. Further, the cardinality of S is n. Ex. $\{13, 100, -17\}$.

A set S is *infinite* whenever there exists an injective mapping $f: S \to S$ such that f(S) is a proper subset of S. Ex. set of natural numbers, set of odd positive integers.

- The proofs for the following are provided in lectures:
 - If a subset S' of S is infinite, then S is infinite.
 - Every subset of a finite set is finite.
 - If S is an inifinite set then the power set of S is infinite.
 - If $f:S\to T$ is an injection and S is infinite, then T is infinite.
- A set S is finite iff S is not infinite.